# Common Misconceptions about Saturation Voltage in Nanoscale MOS Transistors

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## Abstract

Many undergraduate programs in electronic engineering include a one semester course in semiconductor devices. In this course the student is introduced to lumped physical models that are derived from solid-state physics, statistical mechanics and electrostatics for the operating characteristics of transistors and other semiconductor devices. Among the many concepts taught is that the drain-to-source voltage that causes the current flow in an MOS transistor to saturate  $(\partial I_{ds}/\partial V_{ds} \rightarrow 0)$  is given by the simple mathematical expression  $V_{dsat} = V_{gs} - V_T$ . However, this simple expression is widely misapplied by both students and professionals to nanoscale MOS transistors used in modern high-performance microelectronic circuits. This work describes the three competing physical mechanisms that saturate drain-to-source current flow in an MOS transistor and gives a mathematical expression for  $V_{dsat}$  for each mechanism.

### Introduction

The metal-oxide-semiconductor (MOS) transistor is a sandwich-like structure consisting of a semiconductor substrate isolated from a gate electrode by a thin insulating film. A cut-away view of an MOS transistor appears in Figure 1. Modern MOS transistors are typically fabricated from crystalline silicon (Si) substrates and silicon dioxide  $(SiO_2)$  insulating films although other semiconductor substrates, such as gallium arsenide [1] and indium phosphide [2], and other insulating films, such as silicon nitride [3] and aluminum oxide [4], may be used in specialized devices. The gate electrode is usually formed from heavily doped polycrystalline silicon (polysilicon), polysilicon in conjunction with a refractory metal (polycide), or a refractory metal alone. The insulating film is a thin dielectric that is either thermally grown or deposited onto the semiconductor substrate [5] and must be well matched to the crystalline structure of the underlying substrate. A mismatch between the insulator and substrate molecular structures introduces mechanical strain and other asperities [6] at the semiconductor-to-insulator interface that are detrimental to the performance of the transistor [7].

The basic physical features of an n-MOS transistor appear in Figure 1. The n-MOS transistor has two heavily doped n-type regions, the source and drain, at opposite ends of a p-type substrate. Current in an n-MOS transistor consists of a thin layer ( $\approx 10$  Angstroms) of electronic charge that flows from source-to-drain on the semiconductor side of the semiconductor-to-

insulator interface. The thin layer of electronic charge is electrostatically induced by an electric field in the normal direction to the semiconductor surface (the "field effect") that is supported by the application of a gate-to-source voltage ( $V_{gs}$ ). At the same time, charge carriers in the thin layer are driven toward the drain by an electric field in the drain-to-source direction that is supported by the application of a drain-to-source voltage ( $V_{ds}$ ). Conversely, a p-MOS transistor has two heavily doped p-type regions at opposite ends of an n-type substrate and the conducting specie are positively charged holes.



Figure 1: Cut-away view of MOS transistor

Drain-to-source current flow in an MOS transistor can be represented by an equivalent voltage dependent current source. The characteristic response of the current source is given by a monotonic, piecewise smooth and continuous function of the three independent voltages applied across the four terminals of the MOS transistor. The drain-to-source saturation voltage ( $V_{dsat}$ ) is one of the critical points where the "pieces" of the function join.

For fixed values of  $V_{gs}$ , current flow in an MOS transistor saturates at the lowest non-negative value of drain-to-source voltage that either:

- pinches off charge carriers in the conducting channel at the drain junction;
- degrades the mobility of charge carriers in the conducting channel to the extent that drain-to-source current fails to increase with increments of  $V_{ds}$ ;
- or accelerates charge carriers in the conducting channel to their saturation velocities.

Two of these three competing physical mechanisms for saturating transistor current – mobility degradation and velocity saturation [7] – are rarely discussed in introductory courses on semiconductor devices or described in undergraduate textbooks. An incorrect value for  $V_{dsat}$  in an MOS transistor model could introduce a region of negative resistance in the neighborhood of  $V_{dsat}$  that is nonphysical. In a computer simulation of a circuit, this region of negative resistance may cause the circuit simulator to converge to a false solution or, more likely, fail to converge as it endlessly hunts for a stable operating point. This work describes the three physical

mechanisms that saturate drain-to-source current in an MOS transistor and gives a mathematical expression for  $V_{dsat}$  for each mechanism that is appropriate for classroom instruction or for manual calculation.

### Discussion

In the linear and triode regions of operation, where  $V_{gs} \ge V_T$  and  $0 \le V_{ds} \le V_{dsat}$ , the drain-tosource current flow in an MOS transistor is given by

$$I_{ds} = C_{ox} \mu_{eff} \frac{W}{L} \left[ (V_{gs} - V_T) V_{ds} - \frac{1}{2} {V_{ds}}^2 \right].$$
(1)

This simple expression for  $I_{ds}$  is commonly known as the *Spice Level I* transistor model [9]. The notation for the variables and parameters in (1) appears in Table 1. Equation (1) makes use of the simplifying approximation that the areal density of fixed ionic charge in the depletion region beneath the conducting channel is invariant with position along the semiconductor surface [10]. (In this context, the areal density of fixed ionic charge is the net depleted charge per unit area of semiconductor surface.) More complicated *Level II* and *Level III* MOS transistor models include the effects of the variation of depletion charge density with position along the semiconductor surface [6]-[9].

Charge carriers (electrons and holes) are electronically scattered by the nuclei of the background atoms in the semiconductor as they traverse a path from the source to the drain along the semiconductor surface. These scattering events occur sufficiently often that the process for scattering charge carriers at the semiconductor surface can be lumped into an effective mobility parameter in (1) that is given by

$$\mu_{eff} = \left[\frac{1}{L}\int_{0}^{L}\frac{dy}{\mu_{S}}\right]^{-1}.$$
(2)

The functional form for  $\mu_{eff}$  given by (2) is a type of weighted average of the mobility of charge carriers at the semiconductor surface ( $\mu_s$ ) that is assumed in the derivation of (1) [11] and is useful as a parameter in (1) only.

For classroom instruction or for the manual evaluation of  $I_{ds}$ ,  $\mu_{eff}$  in (1) is typically set equal to a constant which omits mobility degradation as a saturating mechanism. However, for practical applications,  $\mu_{eff}$  is given as a function of terminal voltages  $V_{gs}$ ,  $V_{ds}$  and  $V_{bs}$  because the value for  $\mu_s$  is significantly degraded by the electric field in the normal direction [12] that is supported by  $V_{gs}$  and by the electric field in the parallel direction that is supported by  $V_{ds}$  [13]-[15]. Many MOS transistor models used in circuit simulators include the degrading effects of the normal and parallel electric fields upon carrier mobility through the use of a widely accepted empirical function for  $\mu_s$  [11],[16]. Substituting this empirical function for  $\mu_s$  into (2), and invoking the *Level I* simplifying approximation that the density of fixed ionic charge in the depletion region is invariant with position along the semiconductor surface, gives the relation

$$\mu_{eff} = \frac{\mu_0}{1 + \theta_0 (V_{gs} - V_T + 2K\sqrt{\phi_{si} - V_{bs}} - 0.5V_{ds}) + \eta V_{ds}}$$
(3)

where  $\theta_0$ ,  $\eta$  and *K* are parameters that can be extracted from measured transistor characteristics [16],[17]. (It is noteworthy that (3) omits the effects upon  $\mu_{eff}$  introduced by the voltages dropped across the source and drain because of the small parasitic series resistances of these regions although more complicated closed-form expressions for  $\mu_{eff}$  can be derived that include these effects [18].) In the model for effective mobility in (3), the value for  $\mu_{eff}$  decreases as  $V_{bs}$  is made increasingly negative. Some models for  $\mu_{eff}$  described in the engineering literature [19],[20] show the opposite tendency which gives the nonphysical result that  $\mu_{eff}$  increases in value as the value for the normal electric field is made larger with negative increments of  $V_{bs}$ .

Table 1: Table of variables and parameters
Notation
$C_{ox}$ areal capacitance across the gate insulator
$E_{\parallel}$ electric field in the parallel direction
$I_{ds}$ drain-to-source current
$I_{dsat}$ drain-to-source saturation current
K slope of $V_T$ versus $\sqrt{\varphi_{si} - V_{bs}}$ curve
L channel length
$Q_d$ areal density of mobile charge at the drain
<i>V<sub>bs</sub></i> substrate-to-source voltage
$V_{ds}$ drain-to-source voltage
$V_{dsat}$ drain-to-source saturation voltage
$V_{d max}$ value for $V_{ds}$ that maximizes $I_{ds}$
$V_{gs}$ gate-to-source voltage
$V_p$ pinch-off voltage
$V_T$ threshold voltage
$V_{vsat}$ value for $V_{ds}$ that accelerates carriers to $v_{sat}$
$v_{sat}$ saturation velocity of carriers at the surface
W channel width
$\varphi_{si}$ surface potential in strong inversion at source
$\eta$ effective mobility parameter
$\mu_0$ surface mobility for zero electric field
$\mu_{e\!f\!f}$ effective mobility parameter
$\mu_s$ surface mobility
$\theta_0$ effective mobility parameter

#### **Mechanisms for Current Saturation**

As described in the introduction, drain-to-source current in an MOS transistor saturates because of one of three physical mechanisms: pinch-off, mobility degradation, or carrier velocity saturation. This section describes each of these physical mechanisms and gives simple mathematical expressions for  $V_{dsat}$  that are appropriate for classroom instruction or manual calculation.

The areal density of charge carriers in the conducting layer that is electrostatically induced by  $V_{gs}$  varies with position along the channel for values of  $V_{ds}$  that are greater than zero. A sufficiently high value for  $V_{ds}$  can cancel the inductive action of  $V_{gs}$  and cause the conducting layer to vanish near drain end of the conducting channel. If this occurs, the conducting channel is "pinched off" at the drain and the value for  $I_{ds}$  approaches a maximum value, or saturates, for values of  $V_{ds}$  that are greater than the pinch-off voltage [6]-[9]. For a *Level I* model, the areal density of mobile (electronic) charge per unit area of semiconductor surface at the drain end of the conducting channel is given by

$$Q_d = -C_{ox}(V_{gs} - V_T - V_{ds})$$
(4)

for  $V_{gs} \ge V_T$ . The mathematical expression for  $Q_d$  in (4) is consistent with the level of approximation assumed in (1) and (3). The pinch-off voltage  $V_p$  is obtained by setting  $Q_d$  in (4) to zero and solving for  $V_{ds}$  which gives

$$V_p = V_{gs} - V_T . ag{5}$$

The second current saturating mechanism to consider is mobility degradation which can saturate  $I_{ds}$  if  $\mu_{eff}$  is functionally dependent upon  $V_{ds}$ . If the value for  $V_{ds}$  reduces parameter  $\mu_{eff}$  in current equation (1) to the extent that  $I_{ds}$  fails to increase with increments of  $V_{ds}$ , then  $I_{ds}$  saturates because of mobility degradation. Current  $I_{ds}$  in (1) saturates because of mobility degradation at the value of  $V_{ds}$  that maximizes (1) which is determined by substituting the right-hand-side of (3) for  $\mu_{eff}$  into (1), differentiating with-respect-to  $V_{ds}$ , setting the resulting quadratic equation to zero for  $V_{ds} = V_{dmax}$ , and solving for  $V_{dmax}$ . Following this procedure gives

$$V_{d \max} = \frac{B}{2A} \left[ 1 - \sqrt{1 - \frac{4AC}{B^2}} \right]$$
(6)

for parameters A, B and C given by

$$A = 0.5(0.5\theta_0 - \eta),$$
(7a)

$$B = 1 + \theta_0 (V_{gs} - V_T + 2K \sqrt{\varphi_{si} - V_{bs}}) \text{ and}$$
(7b)

$$C = B(V_{gs} - V_T). \tag{7c}$$

Equation (6) gives non-negative Real values for  $V_{d max}$  for the range of values of  $4AC/B^2$  given by  $-\infty < 4AC/B^2 \le 1$ . For  $4AC/B^2 > 1$ , the mechanism of mobility degradation cannot saturate  $I_{ds}$ . If the effect of mobility degradation upon  $I_{ds}$  is omitted by setting  $\mu_{eff}$  equal to a constant  $(\theta_0 = \eta = 0)$ , then

$$\lim_{\mu_{eff} \to \mu_0} V_{d \max} = V_{gs} - V_T \tag{8}$$

and the value for  $V_{d max}$  degenerates to pinch-off voltage  $V_p$  given by (5).

The final current saturating mechanism to consider is velocity saturation. A rigid object that is accelerated by a force field through a viscous medium attains a maximum or terminal velocity when the viscous drag on the object cancels the force that is accelerating the object forward [21]. An analogous situation occurs in the conducting channel of an MOS transistor. Charge carriers that are accelerated by a drain-to-source electric field ( $E_{\parallel}$ ) along a semiconductor surface attain a maximum velocity when the various scattering events along the semiconductor surface cancel the force that is accelerating the carriers toward the drain. These scattering events limit the maximum velocity of charge carriers to the value given by  $\mu_s E_{\parallel}$ . However, the process for increasing the velocity of charge carriers in the channel by increasing the strength of  $E_{\parallel}$  is not unbounded. Eventually, a point is reached where the additional energy supplied by increasing the strength of  $E_{\parallel}$  is primarily emitted by the charge carriers as optical phonons [22] so that any differential change in the value for carrier velocity  $\mu_s E_{\parallel}$  with  $E_{\parallel}$  becomes vanishingly small. The saturation velocity  $v_{sat}$  is the maximum value that  $\mu_s E_{\parallel}$  can attain.

The value for  $v_{sat}$  for charge carriers in the conducting channel of an MOS transistor is critically dependent upon the way that the semiconductor surface was prepared during the fabrication of the transistor. Modern fabrication methods can yield values for  $v_{sat}$  that are as high as 7.9 x10<sup>6</sup> cm/s for MOS transistors operating at room temperature [23] although the value for  $v_{sat}$  can be expected to vary over a wide range of values for different fabrication processes.

The drain-to-source current for charge carriers in the conducting layer that are accelerated to saturation velocity  $v_{sat}$  by drain-to-source voltage  $V_{vsat}$  is given by

$$I_{dsat} = W | Q_d | v_{sat}$$
<sup>(9)</sup>

which, upon substituting the Level I expression in (4) for  $Q_d$ , becomes

$$I_{dsat} = WC_{ox}(V_{gs} - V_T - V_{vsat})v_{sat}.$$
 (10)

Setting the right-hand-side of (10) equal to the right-hand-side of *Level I* current equation (1) for  $\mu_{eff} = \mu_0$  and  $V_{ds} = V_{vsat}$ , and solving the resulting quadratic equation for  $V_{vsat}$  gives [11]

$$V_{vsat} = V_p + \frac{v_{sat}L}{\mu_0} - \sqrt{V_p^2 + \left(\frac{v_{sat}L}{\mu_0}\right)^2}$$
(11)

where the quantity  $V_p$  is the pinch-off voltage given by (5).

It can be shown that (11) only returns positive values for  $V_{vsat}$  by representing the first two terms on the right-hand-side of (11) as the lengths of the sides of a right triangle and noting that the Pythagorean Theorem implies that the term in the square root represents the length of the triangle's hypotenuse. The geometry of the right triangle dictates that the sum of the lengths of the sides is always greater than the length of the hypotenuse which implies that the sum of the first two terms on the right-hand-side of (11) is always greater than the term in the square root which gives the result that  $V_{vsat} > 0$ . Geometric considerations also dictate that the difference between the sum of the lengths of the sides and the length of the hypotenuse of a right triangle is always less than the length of either side of the triangle. This last corollary implies that the maximum value for  $V_{vsat}$  is less than the value of either of the first two terms on the right-hand-side of (11) or, that  $V_{vsat}$  is bounded by  $0 < V_{vsat} < Min [V_p, (v_{sat}L/\mu_0)]$  for the case that  $\mu_{eff}$  is constant ( $\mu_{eff} = \mu_0$ ).

## Conclusion

Three physical mechanisms compete to saturate current flow in an MOS transistor. The physical mechanism that saturates current flow at the lowest drain-to-source voltage "wins" the competition and determines the value of  $V_{dsat}$ . This competitive process is mathematically expressed by the three-way minimum function given by

$$V_{dsat} = \operatorname{Min}(V_p, V_{vsat}, V_{d\max}).$$
(12)

For classroom instruction or for the manual evaluation of  $I_{ds}$ , the complicating effect of mobility degradation upon transistor current flow is often omitted by setting  $\mu_{eff}$  equal to a constant. The elimination of mobility degradation as a current saturating mechanism simplifies the derivation of a mathematical expression for  $V_{dsat}$  by reducing the three-way minimum function in (12) to the two-way minimum function given by  $V_{dsat} = \text{Min}(V_p, V_{vsat})$ . Combining this two-way minimum function with the condition deduced in the prior section that the upper bound on  $V_{vsat}$  is given by  $\text{Min}[V_p, (v_{sat}L/\mu_0)]$  further reduces the three-way minimum function in (12) to  $V_{dsat} = V_{vsat}$  which, upon substituting the right-hand-side of (11) for  $V_{vsat}$ , gives the result

$$V_{dsat} = V_p + \frac{v_{sat}L}{\mu_0} - \sqrt{V_p^2 + \left(\frac{v_{sat}L}{\mu_0}\right)^2}$$
(13)

for the case that  $\mu_{eff}$  is constant ( $\mu_{eff} = \mu_0$ ).

It is instructive to investigate whether the velocity saturation model for  $V_{dsat}$  given by (13) is continuous with the pinch-off model for  $V_{dsat}$  given by (5) for limiting cases where only pinchoff can saturate  $I_{ds}$ . Physical sensibilities dictate that the mechanism of velocity saturation is eliminated for the limiting case where the velocity of carriers at the surface is unbounded  $(v_{sat} \rightarrow \infty)$  as well as for the limiting case where the channel length of the transistor is very long  $(L \rightarrow \infty)$  so that the strength of the electric field in the parallel direction  $(V_{ds}/L)$  is much smaller than the value for the parallel electric field  $(v_{sat}/\mu_0)$  necessary for charge carriers to attain velocity  $v_{sat}$ . For the limiting case where  $v_{sat} \rightarrow \infty$  and for the limiting case where  $L \rightarrow \infty$ , the values for the square root on the right-hand-side of (13) approach the value of  $v_{sat}L/\mu_0$  which respectively give

$$\lim_{v_{sat} \to \infty} V_{dsat} = V_p \quad \text{and} \tag{14a}$$

$$\lim_{L \to \infty} V_{dsat} = V_p \tag{14b}$$

The limiting values for  $V_{dsat}$  given by (14) show that value for  $V_{dsat}$  given by (13) is continuous with the value for  $V_{dsat}$  given by the model for current saturation in (5) that is solely based upon pinch-off. In fact, for a long-channel MOS transistor  $[L >>(\mu_0 V_{dsat} / v_{sat})]$ , (13) returns values for  $V_{dsat}$  that asymptotically approach the values for  $V_{dsat}$  given by (5) as an upper bound. However, modern MOS transistors used in high performance integrated circuits have channel lengths that are measured on the nanometer scale. For these short channel length devices, (13) and (5) can return markedly different values for  $V_{dsat}$  because the first two terms on the righthand-side of (13) can have values that are comparable in magnitude. For a *Level I* MOS transistor model with  $\mu_{eff}$  set to a constant, the correct value for  $V_{dsat}$  is given by (13) instead of the commonly used mathematical expression,  $V_{dsat} = V_{gs} - V_T$ , given by (5) that is valid only for the limiting case of saturation by pinch-off.

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# **Biography**

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